

$$2.1. (g^i h g^j)(g^k h g^l) \dots (g^r h g^s) \\ = g^i h^r g^{j+k+l+\dots+s}$$

2.2.1. only if satisfying axioms

2. isomorphism, each elem. in G map
 to each always same behavior \rightarrow ax.

3. No, $\mathbb{R} \neq \mathbb{Q}$ even tho $|\mathbb{R}| = |\mathbb{Q}|$

2.3. $H \leq G, k \in G$



2.4. $| \langle g \rangle | = | \langle g, g^2, g^3, \dots, g^i \rangle |$

$\therefore n: g^n = g$ (loops back)

Restart when loops $\rightarrow e$

$\hookrightarrow o(g)$

\therefore num elements = $o(g)$

$\hookrightarrow | \langle g \rangle | = o(g) \mathbb{Z}^n$

2.5. $g = (1 \ 5 \ 7) (2 \ 4) \in S_{11}$

$\hookrightarrow | \langle g \rangle | = \{ g, g^2, g^3, g^4, g^5, g^6, g^7 \}$

2.